

## *Simple multivariate analysis 02.sas*

## *The ARIMA Procedure*

Name of Variable = q	
Mean of Working Series	- 0.0034
Standard Deviation	0.999994
Number of Observations	20000

"." marks two standard errors

*Simple multivariate analysis 02.sas*  
*Estimate beta, var(v)*

*The ARIMA Procedure*

Conditional Least Squares Estimation					
Parameter	Estimate	Standard Error	t Value	Approx Pr >  t	Lag
MA1,1	- 0.37391	0.0065612	- 56.99	<.0001	1

Variance Estimate	0.87692
Std Error Estimate	0.93644
AIC	54131.74
SBC	54139.65
Number of Residuals	20000

\* AIC and SBC do not include log determinant.

Autocorrelation Check of Residuals									
To Lag	Chi-Square	DF	Pr > ChiSq	Autocorrelations					
6	2.15	5	0.8286	0.001	0.001	- 0.006	- 0.002	0.008	0.003
12	12.98	11	0.2944	- 0.009	0.001	- 0.006	0.012	- 0.008	- 0.015
18	20.71	17	0.2398	0.005	0.005	0.005	- 0.011	0.012	0.007
24	26.02	23	0.3001	0.002	- 0.001	- 0.012	- 0.008	0.004	0.007
30	31.65	29	0.3352	0.007	- 0.000	0.011	- 0.001	- 0.009	- 0.005
36	37.08	35	0.3734	- 0.003	- 0.001	- 0.013	0.008	0.001	0.006
42	38.22	41	0.5950	- 0.002	- 0.005	0.004	0.001	- 0.000	0.004
48	42.93	47	0.6417	- 0.000	- 0.006	- 0.002	- 0.013	- 0.003	0.005

*Model for variable q*

*No mean term in this model.*

Moving Average Factors	
Factor 1:	1 + 0.37391 B**(1)

*Simple multivariate analysis 02.sas*  
*Estimate beta, var(v)*

*The ARIMA Procedure*

Forecasts for variable q				
Obs	Forecast	Std Error	95% Confidence Limits	
20001	- 0.1961	0.9364	- 2.0315	1.6393
20002	0.0000	0.9998	- 1.9595	1.9595
20003	0.0000	0.9998	- 1.9595	1.9595
20004	0.0000	0.9998	- 1.9595	1.9595
20005	0.0000	0.9998	- 1.9595	1.9595
20006	0.0000	0.9998	- 1.9595	1.9595
20007	0.0000	0.9998	- 1.9595	1.9595
20008	0.0000	0.9998	- 1.9595	1.9595
20009	0.0000	0.9998	- 1.9595	1.9595
20010	0.0000	0.9998	- 1.9595	1.9595
20011	0.0000	0.9998	- 1.9595	1.9595
20012	0.0000	0.9998	- 1.9595	1.9595
20013	0.0000	0.9998	- 1.9595	1.9595
20014	0.0000	0.9998	- 1.9595	1.9595
20015	0.0000	0.9998	- 1.9595	1.9595
20016	0.0000	0.9998	- 1.9595	1.9595
20017	0.0000	0.9998	- 1.9595	1.9595
20018	0.0000	0.9998	- 1.9595	1.9595
20019	0.0000	0.9998	- 1.9595	1.9595
20020	0.0000	0.9998	- 1.9595	1.9595
20021	0.0000	0.9998	- 1.9595	1.9595
20022	0.0000	0.9998	- 1.9595	1.9595
20023	0.0000	0.9998	- 1.9595	1.9595
20024	0.0000	0.9998	- 1.9595	1.9595

## *Simple multivariate analysis 02.sas*

### **The VARMAX Procedure**

Number of Observations	19999
Number of Pairwise Missing	24
Observation(s) eliminated by differencing	1

Simple Summary Statistics							
Variable	Type	N	Mean	Standard Deviation	Min	Max	Difference
p	Dependent	19999	- 0.00152	3.06814	- 8.59261	8.03701	1
q	Dependent	19999	- 0.00345	1.00002	- 1.00000	1.00000	

## Simple multivariate analysis 02.sas

### The VARMAX Procedure

Type of Model	VAR(4)
Estimation Method	Least Squares Estimation

AR Coefficient Estimates			
Lag	Variable	p	q
1	p	- 0.02255	- 0.55074
	q	- 0.00813	0.39899
2	p	- 0.01762	- 0.13625
	q	- 0.00012	- 0.15299
3	p	- 0.01301	0.04180
	q	- 0.00227	0.05408
4	p	- 0.00543	- 0.00937
	q	- 0.00459	- 0.00701

Schematic Representation of Parameter Estimates				
Variable/Lag	AR1	AR2	AR3	AR4
p	.-	..	..	..
q	.+	.-	.+	..
+ is > 2*std error, - is < - 2*stderror, . is between, * is N/A				

Model Parameter Estimates						
Equation	Parameter	Estimate	Standard Error	t Value	Pr >  t	Variable
p	AR1_1_1	- 0.02255	0.02118	- 1.06	0.2870	p(t- 1)
	AR1_1_2	- 0.55074	0.06765	- 8.14	0.0001	q(t- 1)
	AR2_1_1	- 0.01762	0.02113	- 0.83	0.4043	p(t- 2)
	AR2_1_2	- 0.13625	0.07748	- 1.76	0.0787	q(t- 2)
	AR3_1_1	- 0.01301	0.02098	- 0.62	0.5351	p(t- 3)
	AR3_1_2	0.04180	0.07691	0.54	0.5868	q(t- 3)
	AR4_1_1	- 0.00543	0.01165	- 0.47	0.6416	p(t- 4)
	AR4_1_2	- 0.00937	0.04601	- 0.20	0.8386	q(t- 4)
q	AR1_2_1	- 0.00813	0.00663	- 1.23	0.2202	p(t- 1)
	AR1_2_2	0.39899	0.02117	18.84	0.0001	q(t- 1)
	AR2_2_1	- 0.00012	0.00661	- 0.02	0.9854	p(t- 2)

## *Simple multivariate analysis 02.sas*

### *The VARMAX Procedure*

Model Parameter Estimates						
Equation	Parameter	Estimate	Standard Error	t Value	Pr >  t	Variable
	AR2_2_2	- 0.15299	0.02425	- 6.31	0.0001	q(t- 2)
	AR3_2_1	- 0.00227	0.00657	- 0.35	0.7295	p(t- 3)
	AR3_2_2	0.05408	0.02407	2.25	0.0247	q(t- 3)
	AR4_2_1	- 0.00459	0.00365	- 1.26	0.2087	p(t- 4)
	AR4_2_2	- 0.00701	0.01440	- 0.49	0.6265	q(t- 4)

Covariances of Innovations		
Variable	p	q
p	8.95290	2.64155
q	2.64155	0.87719

Information Criteria	
AICC	- 0.132
HQC	- 0.12993
AIC	- 0.132
SBC	- 0.12568
FPEC	0.876341

Cross Covariances of Residuals			
Lag	Variable	p	q
0	p	8.94930	2.64048
	q	2.64048	0.87683

## Simple multivariate analysis 02.sas

### The VARMAX Procedure

Cross Correlations of Residuals			
Lag	Variable	p	q
0	p	1.00000	0.94260
	q	0.94260	1.00000

Schematic Representation of Cross Correlations of Residuals	
Variable/Lag	0
p	++
q	++
+ is > 2*std error, - is < - 2*stderror, . is between	

Univariate Model ANOVA Diagnostics				
Variable	R- Square	Standard Deviation	F Value	Pr > F
p	0.0494	2.99214	148.34	<.0001
q	0.1232	0.93659	401.03	<.0001

Univariate Model White Noise Diagnostics					
Variable	Durbin Watson	Normality		ARCH	
		Chi- Square	Pr > ChiSq	F Value	Pr > F
p	1.99986	1128.70	<.0001	99.88	<.0001
q	1.99964	1801.20	<.0001	437.03	<.0001

Univariate Model AR Diagnostics									
Variable	AR1		AR2		AR3		AR4		Pr > F
	F Value	Pr > F							
p	0.00	0.9961	0.00	0.9998	0.00	1.0000	0.01	0.9999	
q	0.00	0.9816	0.00	0.9992	0.01	0.9993	0.04	0.9972	

## *Simple multivariate analysis 02.sas*

### *The VARMAX Procedure*

Accumulated Impulse Response			
Lag	Variable	p	q
1	p	0.97745	- 0.55074
	q	- 0.00813	1.39899
2	p	0.96481	- 0.89432
	q	- 0.01131	1.40968
3	p	0.95534	- 0.89531
	q	- 0.01350	1.40984
4	p	0.95195	- 0.87631
	q	- 0.01878	1.42414
5	p	0.95563	- 0.88045
	q	- 0.02051	1.43076

Orthogonalized Impulse Response			
Lag	Variable	p	q
0	p	2.99214	0.00000
	q	0.88283	0.31274
1	p	- 0.55367	- 0.17224
	q	0.32793	0.12478
2	p	- 0.34114	- 0.10745
	q	- 0.00008	0.00334
3	p	- 0.02922	- 0.00031
	q	- 0.00641	0.00005
4	p	0.00662	0.00594
	q	- 0.00318	0.00447
5	p	0.00736	- 0.00130
	q	0.00067	0.00207

## Variance Decomposition

Coefficient matrix		
	p	q
p	0.9556281	- 0.88045

Covariance matrix		
	p	q
p	8.9529008	2.6415477
q	2.6415477	0.8771922

Correlation matrix		
	p	q
p	1.000	0.943
q	0.943	1.000

Permutation used in decomposition / ordering of variables:		
p	q	

Permuted coefficients		
	p	q
p	0.9556281	- 0.88045

Permuted covariance matrix		
	p	q
p	8.9529008	2.6415477
q	2.6415477	0.8771922

Cholesky factor of permuted covariance matrix		
	p	q
p	2.9921398	0
q	0.882829	0.3127383

## Variance Decomposition

Variance contributions (ordered)		
	p	q
p	4.335083	0.0758178

Total variance	
p	4.4109008

Proportional contributions		
	p	q
p	0.983	0.017

## Variance Decomposition

Coefficient matrix		
	p	q
p	0.9556281	- 0.88045

Covariance matrix		
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Permuted covariance matrix		
	q	p
q	0.8771922	2.6415477
p	2.6415477	8.9529008

Cholesky factor of permuted covariance matrix		
	q	p
p	0.9365854	0
	2.8204024	0.9991151

## Variance Decomposition

Variance contributions (ordered)		
	q	p
p	3.4992913	0.9116095

Total variance	
p	4.4109008

Proportional contributions		
	q	p
p	0.793	0.207

## Variance Decomposition

Analyze the impact of an initial buy order.

Note: varmax can only construct orthogonalized impulse response functions in the given order of the variables. So we need to re-estimate, placing q first.

## The VARMAX Procedure

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3	q	0.05408	- 0.00227	
	p	0.04180	- 0.01301	
4	q	- 0.00701	- 0.00459	
	p	- 0.00937	- 0.00543	

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	AR3_2_2	- 0.01301	0.02098	- 0.62	0.5351	p(t- 3)
	AR4_2_1	- 0.00937	0.04601	- 0.20	0.8386	q(t- 4)
	AR4_2_2	- 0.00543	0.01165	- 0.47	0.6416	p(t- 4)

Covariances of Innovations		
Variable	q	p
q	0.87719	2.64155
p	2.64155	8.95290

Information Criteria	
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	p	2.64048	8.94930

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Lag	Variable	q	p
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Univariate Model ANOVA Diagnostics				
Variable	R- Square	Standard Deviation	F Value	Pr > F
q	0.1232	0.93659	401.03	<.0001
p	0.0494	2.99214	148.34	<.0001

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Variable	Durbin Watson	Normality		ARCH	
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q	1.99964	1801.20	<.0001	437.03	<.0001
p	1.99986	1128.70	<.0001	99.88	<.0001

Univariate Model AR Diagnostics								
Variable	AR1		AR2		AR3		AR4	
	F Value	Pr > F						
q	0.00	0.9816	0.00	0.9992	0.01	0.9993	0.04	0.9972
p	0.00	0.9961	0.00	0.9998	0.00	1.0000	0.01	0.9999

Accumulated Impulse Response			
Lag	Variable	q	p
1	q	1.39899	- 0.00813
	p	- 0.55074	0.97745
2	q	1.40968	- 0.01131
	p	- 0.89432	0.96481
3	q	1.40984	- 0.01350
	p	- 0.89531	0.95534
4	q	1.42414	- 0.01878
	p	- 0.87631	0.95195
5	q	1.43076	- 0.02051
	p	- 0.88045	0.95563

## Variance Decomposition

Analyze the impact of an initial buy order.

Note: varmax can only construct orthogonalized impulse response functions in the given order of the variables. So we need to re-estimate, placing q first.

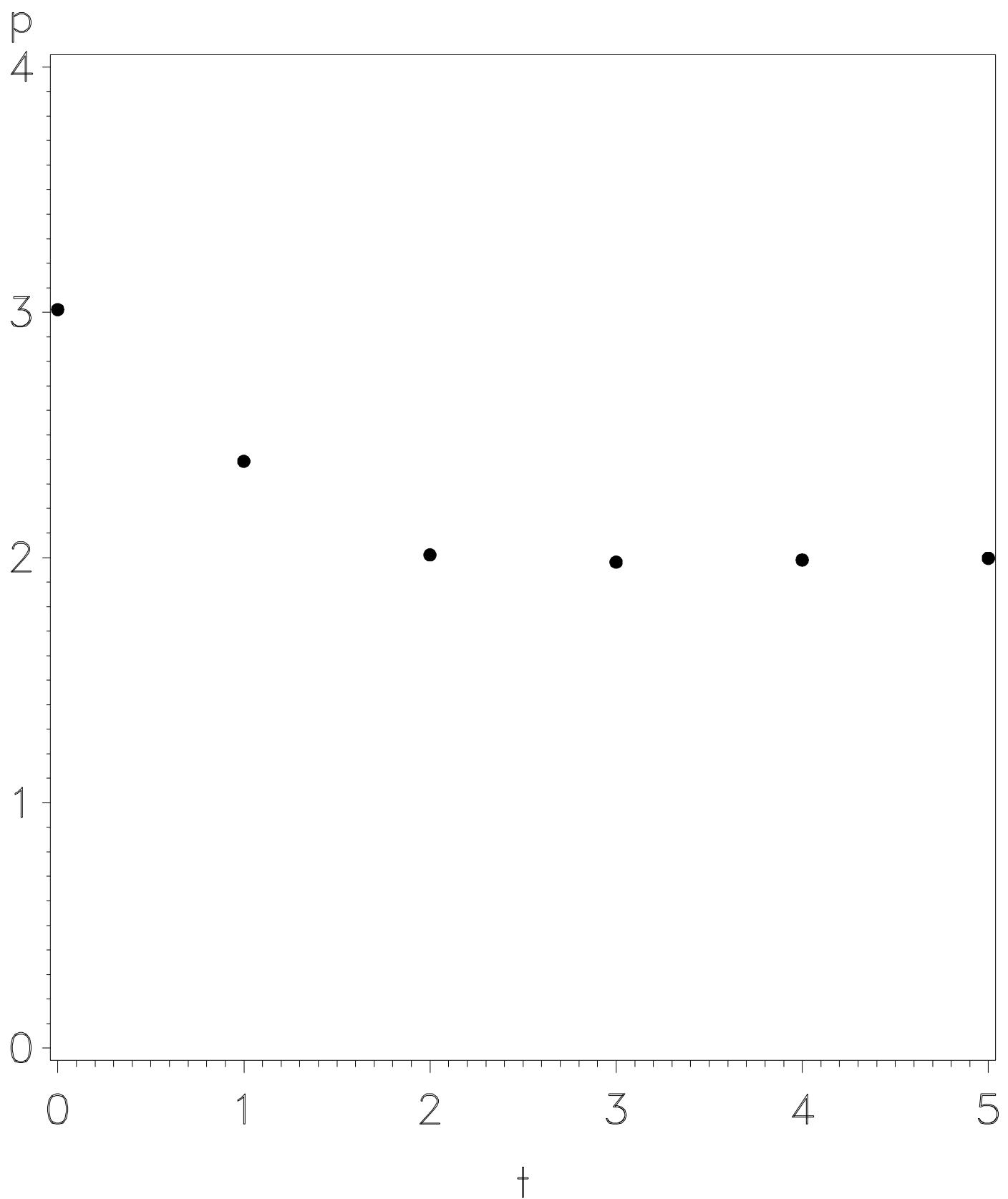
## The VARMAX Procedure

Orthogonalized Impulse Response			
Lag	Variable	q	p
0	q	0.93659	0.00000
	p	2.82040	0.99912
1	q	0.35077	-0.00812
	p	-0.57941	-0.02253
2	q	0.00104	-0.00318
	p	-0.35744	-0.01263
3	q	-0.00603	-0.00219
	p	-0.02765	-0.00946
4	q	-0.00151	-0.00528
	p	0.00822	-0.00339
5	q	0.00132	-0.00173
	p	0.00650	0.00368

*Simple multivariate analysis 02.sas*  
*Impact of a buy order (q=+1 at time 0)*

Obs	q	p	t	qCurrent	pCurrent
1	1.00000	3.01137	0	1.00000	3.01137
2	1.37452	2.39273	1	0.37452	- 0.61864
3	1.37563	2.01109	2	0.00111	- 0.38164
4	1.36919	1.98157	3	- 0.00644	- 0.02952
5	1.36758	1.99035	4	- 0.00161	0.00878
6	1.36899	1.99730	5	0.00141	0.00694

Simple multivariate analysis 02.sas  
Impact of a buy order ( $q=+1$  at time 0)



Simple multivariate analysis 02.sas  
Impact of a buy order ( $q=+1$  at time 0)

